

S where students come first!



Year 12- Mathematics Advanced  
Logarithmic and Exponential Functions

$F = qv \times B$   
 $V_f = V_i + at$   
 $\frac{dy}{dx} = f(x)$   
 $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$   
 $y = f(x)$   
 $(am)^n = a^m n$   
 $AUW = d$   
 $\int t^n dt = \frac{t^{n+1}}{n+1} + C$   
 $v \frac{du}{dt} - u \frac{dv}{dt} = v^2$   
 $a + b + c = \frac{v^2}{2} + v_0 \frac{\Delta t}{2} + \frac{v_0^2}{2}$   
 $\cos e^x$   
 $s_a = \frac{1}{6}k \left(\frac{\Delta t}{2}\right)^3 + v_0 \frac{\Delta t}{2}$   
 $\theta \sin u = \theta \sin u$   
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OFF  
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# Exponential and Logarithms Exam

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1. **(1 marks)**  
Simplify  $e^{2\ln 4}$
2. **(2 marks)**  
If  $f(x) = x^{-e} e^x$ , find  $f'(x)$ .
3. **(2 marks)**  
Find  $\frac{dy}{dx}$  of  $y = \ln(e^2 x^3)$
4. **(2 marks)**  
Find  $\int \left( \frac{e^2}{x} + \frac{x^2}{e} \right) dx$
5. **(2 marks)**  
Find  $\frac{dy}{dx}$  of  $y = e^{-x} \tan x$
6. **(2 marks)**  
Find  $\frac{dy}{dx}$  of  $y = \frac{x^3}{\ln x}$
7. **(4 marks)**  
Find the volume generated when the region enclosed by  $y = 1 - 2e^{2x}$  for  $0 \leq x \leq 2$  is rotated about the x-axis.
8. **(3 marks)**  
Find  $\frac{dy}{dx}$  given  $y = \log_e \left( \frac{2x+1}{3x-7} \right)$
9. **(6 marks)**  
Consider the function  $f(x) = e^{-x} \sin x$  for  $0 \leq x \leq 2\pi$ 
  - i) find the x coordinates where the stationary points occur and determine their nature
  - ii) sketch the curve showing all important features
10. **(6 marks)**  
Sketch the curve  $y = \ln(x + 2)$  and hence find the area in between  $y=0$  and the y-intercept about the y-axis.